

## Are practical mixed-integer linear optimization problems hopeless to solve?

### Peter B. Luh

University of Connecticut,  
Storrs, Connecticut

Email: [peter.luh@uconn.edu](mailto:peter.luh@uconn.edu);

URL: [http://www.ee.uconn.edu/people/faculty/fac\\_luh](http://www.ee.uconn.edu/people/faculty/fac_luh)



### Abstract

Mixed-integer linear optimization problems are prevalent in practical applications, e.g., manufacturing, power, energy, and building systems. Since derivatives of an objective function with respect to discrete decision variables do not exist, there is no necessary optimality conditions. As a result, partial enumeration of discrete variables is generally needed, and the complexity to obtain an optimal solution increases exponentially as the problem size increases. Historically, Lagrangian relaxation was used to solve such problems by relaxing “coupling constraints” and decomposing relaxed problems into subproblems. However, the method suffers major convergence and computational difficulties. The recent trend is to use branch-and-cut that exploits problem linearity. However, complex problems pose major challenges. We developed the Surrogate Lagrangian Relaxation method where a proper direction to update multipliers are obtained without optimally solving all subproblems with much reduced computational efforts and much less multiplier zigzagging. Also, convergence to the optimum does not require the knowledge of the optimal dual value. The method is then synergistically combined with branch-and-cut, allowing

(Abstract Cont.) . Latest developments include Surrogate Augmented Lagrangian Relaxation to further speed up convergence; tightening subproblem formulation with much reduced cutting; and distributed and asynchronous versions for self-optimization applications. The approach opens up a new direction for optimizing mixed-integer linear optimization problems to obtain near-optimal solutions with quantifiable quality in a computationally efficient manner

### Biography

Peter B. Luh received his B.S. from National Taiwan University, M.S. from M.I.T., and Ph.D. from Harvard University. He has been with the University of Connecticut since 1980, and currently is the SNET Professor of Communications & Information Technologies. He is also a member of the Chair Professors Group, Center for Intelligent and Networked Systems (CFINS) in the Department of Automation, Tsinghua University, Beijing, China. Professor Luh is a Life Fellow of IEEE, and the Chair of IEEE TAB Periodicals Committee for the 2018-19 term. He was the VP of Publications of IEEE Robotics and Automation Society (RAS, 2008-2011), the founding Editor-in-Chief of the IEEE Transactions on Automation Science and Engineering (2003-2007), and the Editor-in-Chief of IEEE Transactions on Robotics and Automation (1999-2003). He was the Founding Chair of the Steering Committee of IEEE Conference on Automation Science and Engineering (2006-2011), and continues as a member. His research interests include smart and green buildings, smart power systems, and intelligent manufacturing. He received RAS 2013 Pioneer Award and 2017 George Saridis Leadership Award.

Hosted by: Giulia Pedrielli